

**M.G. KASHI VIDYAPITH, VARANASI**

Three Years Degree Course Syllabus for

## **Statistics**

**(BASED ON UNIFORM SYLLABUS FOR U.P. STATE UNIVERSITIES)**

**(w.e.f. session 2012-13)**

### **Course Instruction**

**B.A./B.Sc. Part-I & Part-II:** There will be three papers of three hours duration of 50 marks in each. Practical will be of 50 marks & three hour duration in each year.

**B.A./B.Sc. Part-III:** There will be three theory papers of three hour duration of 75 marks each. Practical would be of 75 marks & four hours duration.

There will be 9 questions in each paper and candidate has to attempt only 5 questions. Question 1 will be compulsory based on UNIT- I-IV. Two questions will be set from each unit of which one question has to be attempted. All questions will carry equal marks.

**UNIFIED SYLLABUS OF STATISTICS**  
**B.A. / B.Sc. Part- I**

**Paper – I : Probability**

**UNIT – I**

Random experiment, trial, sample point and sample space, events, operations of events, concepts of equally likely, mutually exclusive and exhaustive events. Definition of probability : Classical, relative frequency and axiomatic approaches. Discrete probability space, properties of probability under set theoretic approach. Independence of events, Conditional probability, total and compound probability theorems, Bayes theorem and its applications.

**UNIT – II**

Random variables – discrete and continuous, probability mass function (pmf) and probability density function (pdf), Cumulative distribution function (cdf). Joint distribution of two random variables, marginal and conditional distributions.

**UNIT – III**

Independence of random variables. Expectation of a random variable (rv) and its properties., expectation of sum of random variables and product of independent random variables, conditional expectation and related problems.

**UNIT – IV**

Moments, moment generating function (m.g.f.) & their properties, continuity theorem for m.g.f. (without proof). Chebyshev's inequality. Weak law of large numbers and Central Limit Theorem for a sequence of independently and identically distributed random variables and their applications.

**REFERENCES:**

1. Parzen, E.S. : Modern Probability Theory and its Applications.
2. Meyer, P. : Introductory Probability and Statistical Applications.
3. Stirzeker David (1994) : Elementry Probabilityu, Cambridge University Press.
4. Mood A.M., Graybill F.A. and Boes D.C. (1974) : Introduction to the theory of Statistics, McGraw Hill.
5. Mukhopadhyay, P : Mathmatical Statistics, new central book agency.

## UNIFIED SYLLABUS OF STATISTICS

### B.A/B.Sc. Part- I

#### Paper – II : Probability distributions and Numerical Analysis

##### UNIT – I

Univariate distributions: Binomial, Poisson, Hypergeometric, Geometric and Negative Binomial. Uniform (discrete & continuous), Normal, Exponential, Gamma, Beta distributions. Cauchy, distribution. Normal and Poisson distributions as limiting case of binomial distribution.

##### UNIT – II

Distributions of function of random variables: Distribution of sum, product and quotient of two Variable. Reproductive property of standard distributions.  $\chi^2$ (chi-square), t and F distributions (Central cases only) and their limiting forms. Bivariate normal distribution and its properties.

##### UNIT – III

Calculus of finite differences, operators, separation of symbols, examples and problems. Interpolation formulas with remainder term. Newton's forward and backward formulae. Central difference formulae, Newton's divided difference formulae for interpolation. Lagrange's interpolation formulae.

##### UNIT – IV

Numerical Integration: Derivation of general quadrature formula for equidistant ordinates. Derivation of trapezoidal, Simpson's  $1/3$ rd and  $3/8$ th rules. Weddle's rule. Numerical differentiation using Newton's forward and backward formulae.

##### REFERENCES:

1. Parzen, E.S. : Modern Probability Theory and Its Applications.
2. Meyer, P.: Introductory Probability and Statistical Applications.
3. Freeman : Finite Differences.
4. Scarborough: Numerical Analysis.
5. S.S. Sastry : Introductory Methods of Numerical Analysis; Prentice Hall of India Pvt. Limited.
6. Jain, M.K., Iyengar, SRK and Jain R.K.: Numerical Methods For Scientific And Engineering Computations; NEW AGE International (P) Limited.
7. Saxena, H.C : Calculus of Finite Differences (S. Chand & Co.).

# UNIFIED SYLLABUS OF STATISTICS

## B.A./B.Sc. Part- I

### Paper III Statistical Methods:

#### UNIT-I

Concept of statistical population, Attributes and variables (discrete and Continuous). Primary data – designing a questionnaire and schedule, collection of primary data, checking their consistency. Secondary data. scrutiny of data for internal consistency and detection of errors of recording. Presentation of data: classification, tabulation, diagrammatic & graphical representation of grouped data. Frequency distributions, cumulative frequency distributions and their graphical representations, histogram, frequency polygon and ogives.

#### UNIT-II

Measure of central tendency and dispersion, merits and demerits of these measures. Moments and factorial moments. Shephard's correction for moments. Skewness and Kurtosis and their Measures. Measures based on quartiles. Bivariate data, Method of least squares for curve fitting.

#### UNIT-III

Correlation and regression, rank Correlation ( Spearman's and Kendall's measure), Intra-class correlation, correlation ratio. Partial and Multiple Correlation & Multiple Regression for trivariate data.

#### UNIT-IV

Attributes- Notion and terminology, contingency table, class frequencies, and ultimate class frequencies, consistency. Association of attributes, Independence, Measure of association for 2x2 table. Chi-square, Karl Pearson's and Tschuprow's coefficient of association. Contingency tables with ordered categories.

#### REFERENCES:

1. Goon,Gupta & Dasgupta: Fundamentals of statistics. Vol. I. The world press Private Ltd., Calcutta.
2. Yule, G.U. and Kendall, M.G.: An Introduction to the theory of statistics. Charles Griffin & Company Ltd.
3. C. E. Weatherburn: Mathematical Statistics.

## **B.A./B.Sc. I**

### **PRACTICAL**

The practical examination will be based on papers I, II & III and will cover the following experiments.

#### **List of Practical Experiments**

1. Graphical representation of data by Histogram, Frequency polygons, frequency curves and Ogives. Stem and Leaf Plot, Box Plot.
2. Calculation of measures of location.
3. Calculation of measures of dispersion.
4. Calculation of moments, measures of skewness and measures of Kurtosis.
5. Fitting of curves by method of least squares.
6. Determination of regression lines and calculation of correlation coefficient – grouped and ungrouped data.
7. Calculation of multiple and partial correlation coefficients for three variables
8. Calculation of measures of association in contingency tables.
9. Construction of forward difference tables and divided difference tables.
10. Interpolation by Newton's forward difference formula for equal intervals and calculation of error.
11. Interpolation by Newton's divided difference formula for unequal intervals.
12. Interpolation by Lagrange's formula for unequal intervals.
13. Approximate integration (Trapezoidal rule, Simpson's one-third rule, Simpson's three-eighth rule), Weddle's rule.

**UNIFIED SYLLABUS OF STATISTICS**  
**B.A./B.Sc. Part- II**

**Paper I : Statistical Inference**

**UNIT - I**

Point estimation. Characteristics of a good estimator: Unbiasedness, consistency, sufficiency and efficiency. Method of maximum likelihood and properties of maximum likelihood estimators (without proof). Method of minimum Chi-square. Method of Least squares and method of moments for estimation of parameters. Problems and examples.

**UNIT - II**

Sufficient Statistics, Cramer-Rao inequality and its use in finding MVU estimators. Statistical Hypothesis (simple and composite). Testing of hypothesis. Type I and Type II errors, significance level, p-values, power of a test. Definitions of Most Powerful (MP), Uniformly Most Powerful (UMP) and Uniformly Most Powerful Unbiased (UMPU) tests.

**UNIT - III**

Neyman-Pearson's lemma and its applications for finding most powerful tests for simple hypothesis against simple alternative. Tests based on t, F and  $\chi^2$  distributions.

**UNIT-IV**

Large sample tests. Interval estimation, Pivotal quantity and its use in finding confidence intervals, concept of best confidence intervals.

**REFERENCES:**

1. Hogg & Craig : Mathematical Statistics.
2. Mood, Graybill and Boes : Introduction to the theory of Statistics.
3. Goon, Gupta and Dasgupta : Fundamentals of Statistics Vol.1 & II
4. Ferund J.E (2001) : Mathmatical Statistics, Prentice Hall of India.

## UNIFIED SYLLABUS OF STATISTICS

### B.A./B.Sc. Part- II

#### Paper II : Survey Sampling

##### UNIT - I

Sampling vs. complete enumeration : sampling units and frame. Precision and efficiency of estimators. Simple Random sampling with and without replacement. Use of random number tables in selection of simple random sample. Estimation of population mean and proportion. Derivation of expression for variance of these estimators. Estimation of variances. Sample size determination.

##### UNIT-II

Stratified random sampling. Problem of allocation, proportional allocation, optimum allocation. Derivation of the expressions for the standard errors of the usual estimators when these allocations are used. Gain in precision due to stratification. Role of sampling cost in the sample allocation. Minimization of variance for fixed cost.

##### UNIT-III

Systematic sampling : estimation of population mean and population total, standard errors of these estimators. Regression and ratio methods of estimation in simple random sampling.

##### UNIT-IV

Cluster sampling with equal clusters: estimators of population mean and their mean square error. Two-stage sampling with equal first stage units : estimator of population mean and its variance. Concept of Non-sampling errors.

##### REFERENCES:

1. Cochran, W.G. : Sampling Techniques
2. Sukhatme, Sukhatme, Sukhatme & Asok : Sampling Theory of Surveys with applications.
3. Murthy, M. N. : Sampling theory.

## UNIFIED SYLLABUS OF STATISTICS

### B.A./B.Sc. Part- II

#### **Paper III : Analysis of Variance and Design of Experiment.**

##### **UNIT-I**

Analysis of Variance. One way classification. Assumptions regarding model. Two way classification with equal number of observations per cell.

##### **UNIT-II**

Principles of Design of experiments: Randomization, Replication and local control. Choice of size and type of a plot using uniformity trials. CRD, Randomized block design. Concept and definition of efficiency of design. Comparison of efficiency between CRD and RBD.

##### **UNIT - III**

Latin square Design, Lay-out, ANOVA table. Comparison of efficiencies between LSD and RBD; LSD and CRD. Missing plot technique : estimation of missing plots by minimizing error sum of squares in RBD and LSD with one or two missing observations.

##### **UNIT-IV**

Factorial Experiments : general description of factorial experiments;  $2_2$ ,  $2_3$  and  $2_n$  factorial experiments arranged in RBD. Definition of main effects and interactions in  $2_2$  and  $2_3$  factorial experiments. Preparation of ANOVA by Yates procedure. Estimates and tests for main and interaction effects (Analysis without confounding).

##### **REFERENCES:**

1. Cochran and Cox : Experimental Design
2. Kempthorne : Design of Experiments
3. Federer : Experimental Designs
4. Goon, Gupta and Dasgupta : Fundamentals of Statistics, Vol. II
5. Das & Giri : Design and Analysis of Experiments (Wiley Eastern).



**B.A./B.Sc. Part- II**  
**PRACTICAL**

The practical examination will be based on papers I, II and III and will cover the following experiments:

**List of Practical Experiments**

1. Fitting of Binomial, Poisson and Normal distributions to observed data and testing of goodness of fit.
2. Testing of independence of attributes in  $m \times n$  contingency table and calculation of measures of association.
3. t - test for (i)  $\mu = \mu_0$  (ii)  $\mu_1 = \mu_2$  (iii)  $\rho = \rho_0$
4. F-test for  $\sigma_1 = \sigma_2$
5. Fisher's Z-transformation and its use in testing (i)  $\rho_1 = \rho_2$  (ii)  $\rho = \rho_0$
6. Calculation of power curve for the test of  $\mu = \mu_0$  against  $\mu \neq \mu_0$  for a normal distribution with known variance.
7. Large sample tests.
8. Analysis of variance in one-way and two-way classification (with and without interaction terms).
9. Analysis of a Latin square design.
10. Analysis of variance in RBD and LS design with one or two missing observations.
11. Drawing a simple random sample with the help of table of random numbers.
12. Estimation of population means and variance in simple random sampling.
13. Stratified random sampling for population mean (proportional and optimum allocation).
14. Ratio and regression estimation of population mean and total.
15. Factorial Experiment Practical.

## UNIFIED SYLLABUS OF STATISTICS

### B.A. / B.Sc. Part- III

#### **Paper 1 : Non-parametric Methods and Computer Programming in C**

##### **UNIT - I**

Order Statistics. Distributions of minimum,  $r^{\text{th}}$  and maximum order statistic. Joint distribution of  $r^{\text{th}}$  and  $s^{\text{th}}$  order statistics (in continuous case) Distribution of sample range & sample median, for uniform and exponential distributions.

##### **UNIT - II**

Non-parametric tests – Tests for randomness and test for goodness of fit. One sample tests : sign test, Wilcoxon signed rank tests. Two sample tests : run test, Kolmogorov – Smirnov's test, Median test and Mann-Whitney U test, Spearman's rank correlation test.

##### **UNIT - III**

Programming preliminaries, Structure of a C program, Small program in C, Numerical constant and variable, Arithmetic and Assignment expressions and their use, Input and output functions.

##### **UNIT - IV**

Conditional Statements in C – Loops - while loop, for loop and do while loops, Array.

##### **REFERENCES :**

1. Mood, A.M., Graybill F and Boes D.C. : Introduction to the theory of Statistics.
2. Gibbons, J.D. : Non-parametric statistical inference
3. Conover, W.J. : Practical Non-parametric Statistics
4. David, H.A. : Order Statistics
5. Rajaraman,V. :Computer Programming C

**UNIFIED SYLLABUS OF STATISTICS**  
**B.A. / B.Sc. Part- III**

**Paper II : Applied Statistics**

**UNIT - I**

Time series, its different components, illustrations, additive and multiplicative models, determination of trend, growth curves, analysis of seasonal fluctuations, construction of seasonal indices. Idea of Correlogram & periodogram. Index number – its definition, application of index number, price relative and quantity or volume relatives, link and chain relative, problem involved in computation of index number, use of averages, simple aggregative and weighted average method. Laspeyre's, Paashe's and Fisher's index number, time and factor reversal tests of index numbers, consumer price index

**UNIT - II**

Educational Statistics: Scaling procedures – scaling of test items, test scores, rating of qualitative answers and judgements. Test theory, linear models, parallel tests, true score, reliability and validity of tests. Tetra-choric, bi-serial and point bi-serial correlation coefficients.

**UNIT - III**

Demographic methods : Sources of demographic data – census, register, ad-hoc survey, hospital records, demographic profiles of Indian Censuses. Measurement of mortality, crude death rates, age specific death rates, infant mortality rates, standardized death rates. Measurement of fertility – crude birth rate, general fertility rate, age-specific birth rate, total fertility rate, gross reproduction rate, net reproduction rate,. Logistic curve fitting and its use in population projection. Complete life table, its main features and construction. Official Statistics CSO, NSSO and census organizations their set-up and functions.

**UNIT - IV**

Control charts for variables and attributes, modified control charts, group control charts, Sampling inspection by attributes – single and double sampling plans.Producer's and consumer's risk, OC, ASN functions AOQL and LTPD of sampling plans. Sampling inspection by variables – simple cases.

**REFERENCES :**

1. Montgomery D.C. (1985) : Introduction to Statistical Quality Control (Wiley).
2. Draper & Smith : Applied Regression Analysis
3. Burr : Industrial Quality Control.
4. Wetherill and Brown : Statistical Quality Control
5. Croxton F.E. and Cowden D.J. : Applied General Statistics
6. Goon, Gupta and Dasgupta : Fundamentals of Statistics, Vol. I & II
7. Siya Ram : Applied Statistics.

## UNIFIED SYLLABUS OF STATISTICS

### B.A. & B.Sc. Part- III

#### Paper III : Operations Research

##### UNIT - I

General linear programming problems and their formulations. Method for solving LPP : Graphical Method, Simplex method, Big - M method, Two phase Method Duality in LPP  
Transportation problem: North-west corner rule, Least cost method, Vogel's approximation method(feasible solution). Assignment Problem : Hungarian Algorithm.

##### UNIT - II

Elements of games, Zero sum two person games, Saddle point, Optional strategies, Maximin- minimax principle of rectangular games, Games without saddle point, Graphical solution of  $2 \times N$  or  $M \times 2$  games, Solution of game by dominance principles, Reduction of game to LPP.

##### UNIT - III

Replacement problems (individual and group). Queueing Models - M/M/1, M/M/C models waiting time distribution for M/M/1, Little's formulae. M/G/1 Queueing system, cost profit models in queueing theory.

##### UNIT - III

Inventory Models : EOQ models, Non-zero, lead time, EOQ with shortages allowed. Job sequencing : n jobs - machines, n jobs - K machines, 2 jobs - n machines.

##### REFERENCES :

1. Swarup Kanti, Gupta P.K. and Man Mohan : Operations Research, Sultan Chand & Sons.
2. Taha, H.A. : Operations Research, Mac Millan publishing.

##### PRACTICALS :

Based on Paper I, Paper II and Paper III.